

Research Paper

ALTERATION OF BASALT AND CALCAREOUS AGGREGATES' ROUNDNESS WITH DIFFERENT ABRASION METHODS

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In concrete and asphalt concrete, the shape (roundness) of aggregate particles has been related to durability, workability, shear resistance, tensile strength, stiffness, and fatigue response. The aggregates are constantly subjected to harsh environmental conditions and external forces including static and dynamic loads. As a result, these materials experience various levels of abrasion. Hence, alteration of aggregate roundness with different chemical and mechanical effects is important for engineers. In this research, 40 basalt and calcareous aggregate samples are prepared with different abrasion methods and the roundness of samples is determined using image analysis. As a result, calcareous aggregate is significantly affected from the abrasion methods but basalt aggregate is not.

Keywords: Roundness, Basalt aggregate, Calcareous aggregate, Abrasion, Image analysis

INTRODUCTION

The particle shape characteristics of the aggregate significantly affect the workability, strength, and durability of the concrete (Ozol, 1978; Kwan *et al.*, 1999; Erdogan, 2005; Erdogan *et al.*, 2006) and asphalt concrete (Kuo *et al.*, 1996; Masad *et al.*, 2001; Al-Rousan *et al.*, 2007; Odurroh *et al.*, 2000). Another important characteristic of aggregate that affects concrete properties is the resistance to degradation. Aggregates are exposed to impact and/or abrasion forces

during plant operations and compaction. These forces might cause changes in aggregate size distribution leading to field produced mixes different from the laboratory designed ones (Wu *et al.*, 1998). The construction and traffic loading could also cause aggregate abrasion leading to the loss of aggregate angularity, which weakens the mix resistance to applied loads (Gatchalian *et al.* (2006; Enad and Masad, 2007).

In recent years, image analysis has been used in widespread applications in many

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disciplines, such as medicine, biology, geography, meteorology, manufacturing, and material science. But, there have been relatively fewer applications of image analysis used in civil engineering. Imaging technology has been used recently to quantify aggregate shape characteristics and several researchers had investigated the role of aggregate shape in concrete and asphalt mixture (Erdogan, 2005; Masad *et al.*, 2001; Al-Rousan *et al.*, 2007; Masad and Button, 2000; Masad *et al.*, 2000; Masad *et al.*, 2005). Some of these studies have focused on characterizing the 3D shape of aggregates (Erdogan *et al.*, 2006; Garboczi, 2002; Garboczi and Bullard, 2004; Fernlund, 2005a; Fernlund, 2005b). Others have investigated the determination of shape properties of aggregate (Kwan *et al.*, 1999; Mora and Kwan, 2000) and grain size distribution (Fernlund, 1998; Mora *et al.*, 1998; Mertens and Elsen, 2006). Also, others have been devoted to developing procedures to describe the shape of aggregates with an emphasis on elongation or form (Barksdale *et al.*, 1991; Rao and Tutumluer, 2000), angularity (Masad *et al.*, 2000; Yudhbir and Abedinzadeh, 1991; Kuo and Freeman, 2000), and texture (Masad and Button, 2000; Hryciw and Raschke, 1996).

As mentioned above, the importance of the roundness and resistance to degradation of aggregate particles on the performance of concrete and asphalt concrete is also well recognized. For this reason, the present study was undertaken to investigate the effect of different abrasion methods to the roundness of basalt and calcareous aggregates using image analysis.

ROUNDNESS OF AGGREGATE

Particle geometry can be fully expressed in terms of three independent properties: form roundness (or angularity), and surface texture. Form, roundness and surface texture are also essentially independent properties of shape because one of them can vary widely without necessarily affecting the other two properties (Barrett, 1980). Particle roundness relates to the relative rounding or angularity (sharpness) of corners and edges (Barrett, 1980; Masad, 2004; Blott and Pye, 2008; Wadell, 1932; Pryor, 1971; Pettijohn *et al.*, 1972).

Most authors proposed charts for determination of particle roundness (Rittenhouse, 1943; Krumbein and Sloss, 1963; Powers, 1953; Alshibli and Alsales, 2004; Powers, 1982). Previous studies had estimated roundness using visual comparison scales (Mackie, 1897; Dunn, 1911). One of the first attempts to quantify the roundness of particles was made by Wentworth (1919). He noted that roundness was dependent on the radius of curvature of the corners of a particle. Different researchers were also using different roundness indexes to describe the shape of particles and even different definitions for the same roundness index (Wadell, 1932; Powers, 1953; . Wentworth, 1922b; Wentworth, 1922c; Cox, 1927; Wadell, 1933; Wadell, 1935; Cailleux, 1947; Dobkins and Folk, 1970; Al-Rousan, 2004; Mitchell and Soga, 2005). Roundness is defined as (Cox, 1927):

$$R(\text{Roundness}) = \frac{4 \cdot \Pi \cdot A}{P^2} \quad \dots(1)$$

This is a shape factor that has a minimum value of 1 for a circle and lower values for

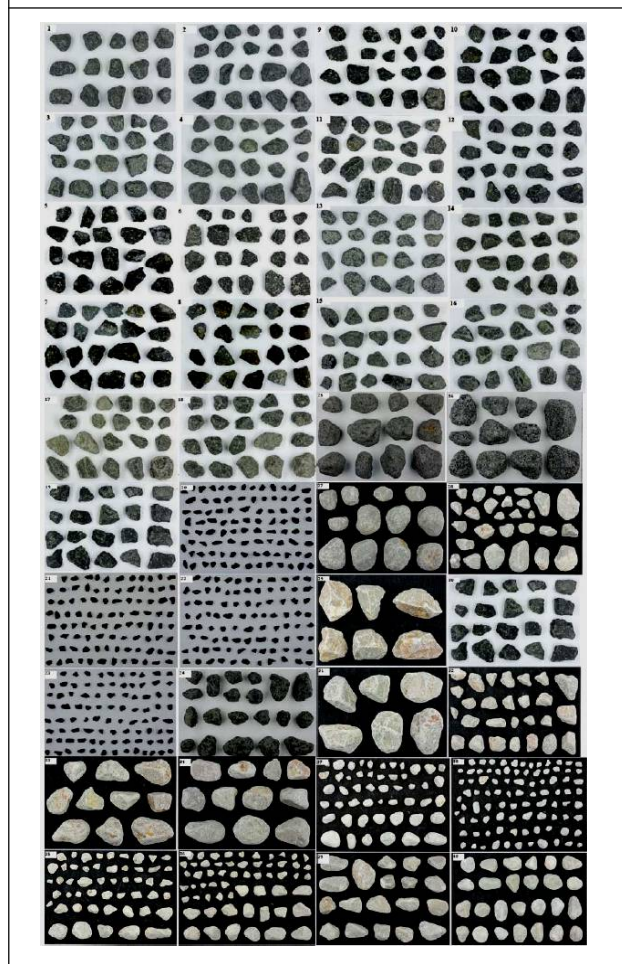
shapes having a higher ratio of area (A) to perimeter (P), longer or thinner shapes, or objects having rough edges.

MATERIALS AND METHODS

Crushed basalt and calcareous aggregate were used in this study. The specific gravities of basalt and calcareous aggregates were found 2.90 and 2.62 according to ASTM D 854, respectively. The imaging system used by the authors consists of a Nikon D80 Camera and Micro 60 mm objective manufactured by Nikon. 100 particles were selected for each aggregate fraction and placed within the sample tray for capturing the images. The output of camera was a 3872-2592 pixel, 32-bit digital image of RGB color. The particles had to be identified prior to analysis. Image J was used as the image analysis program. Threshold gray intensity therefore had to be chosen. Thresholding determines the outline of the aggregate particle in a captured image. Clearly, the particle should have a sharp contrast against the background to accurately delineate the actual boundaries. A threshold value of pixel gray level is typically specified, and the actual image is converted to a binary image. This binary image has only black or white (gray level 0 or 255) pixels to clearly identify the particle against its background. The gray intensity measured on a given point was compared to the threshold value. Then, the initial gray image was converted into a binary image in which the aggregate particles that have lower gray intensity than the threshold value were set to black while the background was set to white. Applying a global threshold value for all the image worked well only if the objects of interest (aggregate particles) had

uniform interior gray level and rested upon a background of different, but uniform, gray level. This was made possible in this study by placing particles on white background. After then, output data of ImageJ was transferred to Excel. The output data also contain area, perimeter, L, I, and S values of view of each aggregate in unit of millimeter, and quantity of aggregates. The other properties of used materials test procedures, imaging system and digital image

Figure 1: Image Samples of Aggregates



processing steps were also detailed in previously researches of authors (Arasan et al., 2011; Arasan et al., 2011; Polat et al., 2013).

Table 1: Roundness Value and Class of Aggregate Samples

| No. | Aggregate | Method | R | Class |
|-----|-----------|--|-------|--------------|
| 1 | Basalt | Los Angeles Rattler Machine without steel balls-mixed gradation-number of revolution is 200.000 | 0,796 | Sub Rounded |
| 2 | Basalt | Los Angeles Rattler Machine without steel balls-mixed gradation-number of revolution is 80.000 | 0,784 | Sub Rounded |
| 3 | Basalt | Los Angeles Rattler Machine without steel balls-not mixed gradation-number of revolution is 3.000 | 0,670 | Angular |
| 4 | Basalt | Los Angeles Rattler Machine without steel balls-not mixed gradation-number of revolution is 35.000 | 0,750 | Sub Angular |
| 5 | Basalt | Treated with sulfuric acid | 0,648 | Very Angular |
| 6 | Basalt | Rotating with vertical concrete mixer (30 second) | 0,666 | Angular |
| 7 | Basalt | Treated with sulfuric and nitric acids | 0,697 | Angular |
| 8 | Basalt | Treated with nitric acid | 0,703 | Angular |
| 9 | Basalt | M Rotating with vertical concrete mixer (one hour) | 0,761 | Sub Rounded |
| 10 | Basalt | Treated with salt solution | 0,682 | Angular |
| 11 | Basalt | Los Angeles Rattler Machine without steel balls-mixed gradation and treated with salt solution-number of revolution is 6.000 | 0,653 | Angular |
| 12 | Basalt | Los Angeles Rattler Machine without steel balls-not mixed gradation-number of revolution is 1.000 | 0,672 | Angular |
| 13 | Basalt | Los Angeles Rattler Machine without steel balls-mixed gradation-number of revolution is 6.000 | 0,725 | Sub Angular |
| 14 | Basalt | Los Angeles Rattler Machine without steel balls-mixed gradation-number of revolution is 30.000 | 0,688 | Angular |
| 15 | Basalt | Los Angeles Rattler Machine with five steel balls-mixed gradation-number of revolution is 500 | 0,586 | Very Angular |
| 16 | Basalt | Los Angeles Rattler Machine without steel balls-mixed gradation-number of revolution is 90.000 | 0,752 | Sub Rounded |
| 17 | Basalt | Los Angeles Rattler Machine without steel balls-mixed gradation-number of revolution is 80.000 | 0,611 | Angular |
| 18 | Basalt | Los Angeles Rattler Machine without steel balls-mixed gradation-number of revolution is 45.000 | 0,722 | Sub Angular |
| 19 | Basalt | Raw Aggregates | 0,664 | Angular |
| 20 | Basalt | Los Angeles Rattler Machine with 50% abrasive balls-mixed gradation-number of revolution is 5.000 | 0,721 | Sub Angular |

Table 1 (Cont.)

| No. | Aggregate | Method | R | Class |
|-----|------------|--|-------|--------------|
| 21 | Basalt | Los Angeles Rattler Machine with 50% abrasive balls-mixed gradation-number of revolution is 33.000 | 0,735 | Sub Angular |
| 22 | Basalt | Los Angeles Rattler Machine with 20% abrasive balls-mixed gradation-number of revolution is 20.000 | 0,745 | Sub Angular |
| 23 | Basalt | Los Angeles Rattler Machine with 12% abrasive balls-mixed gradation-number of revolution is 50.000 | 0,755 | Sub Rounded |
| 24 | Basalt | Los Angeles Rattler Machine with 50% bearing balls (bigger than aggregate)-mixed gradation-number of revolution is 5.000 | 0,782 | Rounded |
| 25 | Basalt | Los Angeles Rattler Machine with 50% bearing balls (smaller than aggregate)-mixed gradation-number of revolution is 33.000 | 0,784 | Rounded |
| 26 | Basalt | Los Angeles Rattler Machine with 50% bearing balls (smaller than aggregate)-mixed gradation-number of revolution is 40.000 | 0,772 | Rounded |
| 27 | Calcareous | Los Angeles Rattler Machine with 50% bearing balls (smaller than aggregate)-mixed gradation-number of revolution is 13.000 | 0,852 | Well Rounded |
| 28 | Calcareous | Los Angeles Rattler Machine without steel balls-mixed gradation-number of revolution is 13.000 | 0,793 | Rounded |
| 29 | Calcareous | Raw Aggregates | 0,725 | Sub Angular |
| 30 | Basalt | Raw Aggregates | 0,664 | Angular |
| 31 | Calcareous | Los Angeles Rattler Machine without steel balls-not mixed gradation-number of revolution is 2.000 | 0,798 | Rounded |
| 32 | Calcareous | Los Angeles Rattler Machine without steel balls-not mixed gradation-number of revolution is 35.000 | 0,784 | Rounded |
| 33 | Calcareous | Los Angeles Rattler Machine without steel balls-two gradation-number of revolution is 13.000 | 0,782 | Rounded |
| 34 | Calcareous | Los Angeles Rattler Machine without steel balls-two gradation-number of revolution is 40.000 | 0,818 | Well Rounded |
| 35 | Calcareous | Los Angeles Rattler Machine without steel balls-aggregates are smaller than 10mm-number of revolution is 30.000 | 0,785 | Rounded |
| 36 | Calcareous | Los Angeles Rattler Machine without steel balls-aggregates are smaller than 10mm-number of revolution is 50.000 | 0,798 | Rounded |
| 37 | Calcareous | Los Angeles Rattler Machine without steel balls-aggregates are smaller than 10mm-number of revolution is 80.000 | 0,827 | Well Rounded |
| 38 | Calcareous | Los Angeles Rattler Machine without steel balls-aggregates are smaller than 5mm-number of revolution is 30.000 | 0,825 | Well Rounded |
| 39 | Calcareous | Los Angeles Rattler Machine without steel balls-consecutive two aggregates -number of revolution is 50.000 | 0,798 | Rounded |
| 40 | Calcareous | Los Angeles Rattler Machine without steel balls-consecutive two aggregates -number of revolution is 100.000 | 0,848 | Well Rounded |

RESULTS AND CONCLUSION

Forty different methods were attempted to basalt and calcareous aggregates for alteration of aggregate roundness with different chemical and mechanical effects. The roundness of samples was determined using and image analysis Equation 1 as described previously. Additionally, the roundness classes of samples were determined by using modified Powers (1953) chart mentioned in Arasan (2011). The roundness values and classes of raw basalt and calcareous aggregates were 0.664, 0.725 and angular, sub-angular, respectively. The images of samples were given in Figure 1. The attempted methods were numbered and these numbers given in figures. It is seen from figures that the roundness of calcareous samples were significantly changed but basalt samples were not.

The samples roundness values, classes and description of applied methods were given in Table 1. Additionally, some significant conclusions were summarized below:

- The raw basalt aggregate had lower roundness value and more angular than calcareous aggregate.
- Sulfuric acid abraded the aggregates and the aggregates became more angular (Method 5).
- Nitric acid and salt solutions did not significantly affect aggregates (Method 7, 8 and 10).
- The sulfuric and nitric acids were melted calcareous aggregate. This result was not given in Table 1.

- If the aggregates (basalt and calcareous) were rotated in Los Angeles Rattler Machine with steel balls, the aggregates crushed and became smaller.
- If the aggregates (basalt and calcareous) were rotated in Los Angeles Rattler Machine without steel balls, the aggregates did not crush and became rounded.
- If the (basalt and calcareous) aggregates were rotated in Los Angeles Rattler Machine with abrasive or bearing balls, the aggregates became rounded.
- If the diameter of abrasive or bearing balls was bigger than aggregate diameter, the aggregates crushed and became smaller.
- The number of revolutions for Los Angeles Rattler Machine significantly affected the level of abrasion.
- The basalt aggregates were more resistant than calcareous aggregate when abrasion put into consideration.

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